

(N.B. See section 7.6 of your textbook)

**FYI**

**GRAPHING & SOLVING  
SYSTEMS OF  
LINEAR INEQUALITIES**



A **system of linear inequalities** is simply two or more related linear inequalities that are graphed in the same coordinate plane.

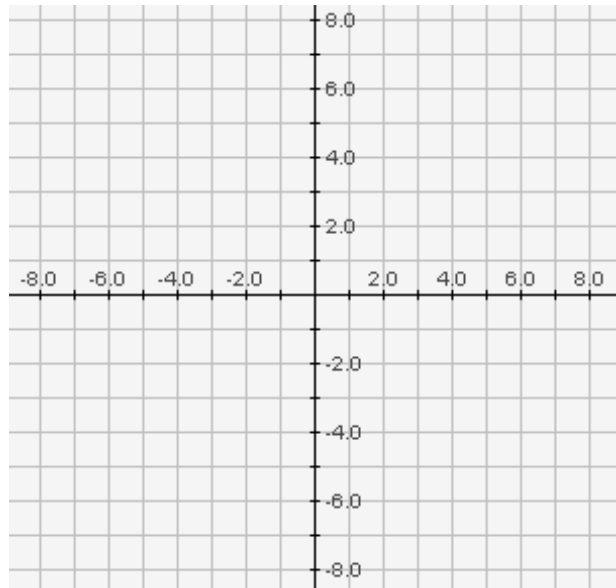
The **SOLUTION** for a system of linear inequalities is the set of all ordered pairs that satisfy both (or all) of the inequalities. This set of points is called the **SOLUTION REGION**.

The **SOLUTION REGION** is the **INTERSECTION** of the individual half-plane solutions of each inequality.

Example 1: Sketch the graph of the system of linear inequalities and shade the solution region.

$$y < 2$$

$$y \geq \frac{1}{2}x - 2$$



Hint: First graph the boundary lines (equations) for  $y = 2$  and  $y = \frac{1}{2}x - 2$

**Caution! Dashed Line or Solid Line??**

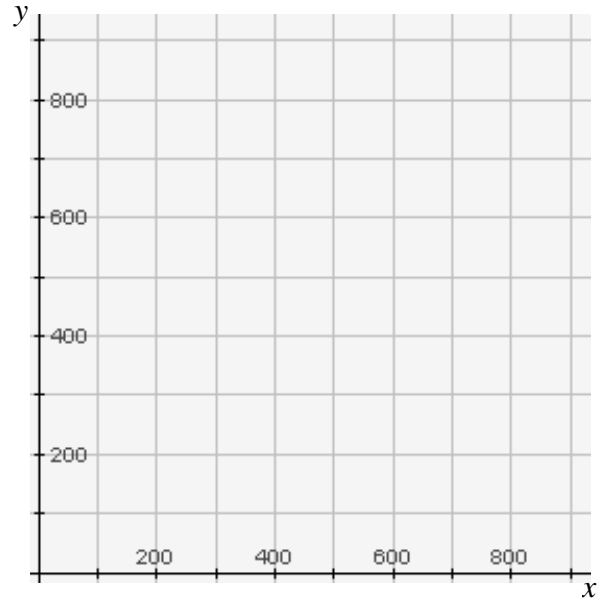
Second, lightly mark or shade each half-plane

Third, shade the intersection of the half-planes

**Recall from Problem Set 6A...**

1. Last Friday night, **more than** \$1875 was paid at the gate of the high school football game. Student tickets were sold for \$3.00 and adult tickets for \$5.00.  
**New Information!** The maximum capacity of the stadium is 900 people.

a) Write two inequalities that describe this situation in terms of the number of students,  $x$ , and the number of adults,  $y$ .



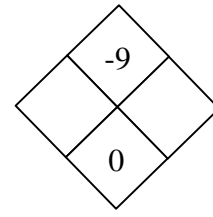
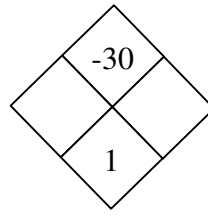
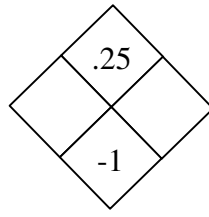
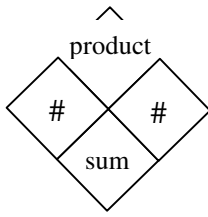
b) Using your inequalities as if they were equations, find the  $x$ - and  $y$ -intercepts for each inequality.

$$\begin{array}{c|c} x & y \\ \hline 0 & 0 \end{array}$$

$$\begin{array}{c|c} x & y \\ \hline 0 & 0 \end{array}$$

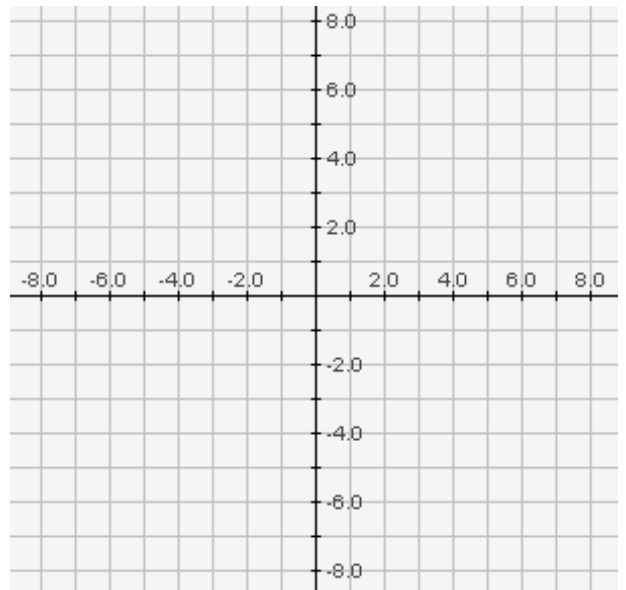
c) Sketch a graph of the system of inequalities that highlights the possible combinations of adults and students that attended the game.  
**Label the axes and shade the solution region.**

2. Solve each of the following diamond problems:

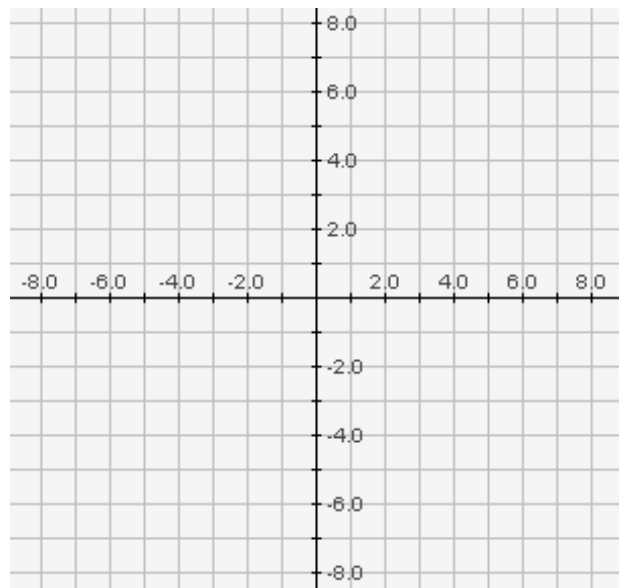


3. Sketch a graph of the systems of inequalities. Show all work.

a)  $y > -4$   
 $y \geq 2x + 1$   
 $x \geq -6$



b)  $x < -1$   
 $x \geq -7$   
 $y < 6$   
 $y \geq -3$



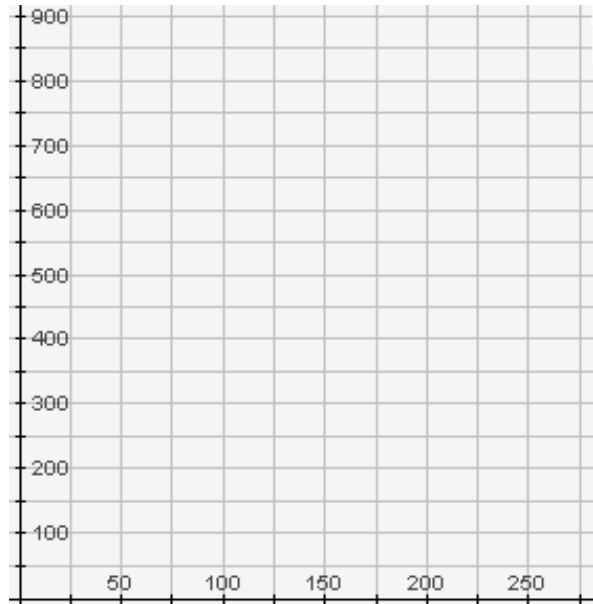
4. The student government association held a fundraising dance to raise money for the Washington D.C. trip. The Home-School Association donated \$100 in cash. Students were each charged \$3 admission.

**New Information #1:** The students held a bake sale at the dance that, if it sold out, could generate as much as another \$200 profit.

**New Information #2:** A maximum of 250 students were allowed to attend.

Sketch a graph that shows ALL of the possibilities for money raised.

- a) Write **THREE** (3) linear inequalities that describe this situation.  
Let the **x-axis** represent the number of students attending  
Let the **y-axis** represent the amount of money raised.

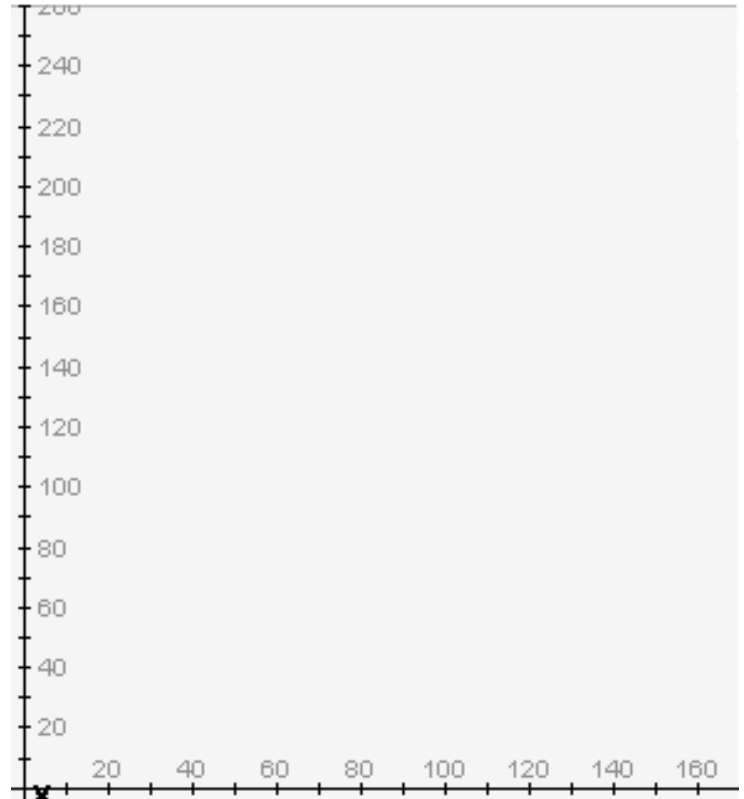


- b) Sketch a graph of the boundary lines and shade the region of the graph that shows the possible solutions for total money raised. **LABEL THE AXES accordingly.**
- c) Use the **TEST POINTS** method to confirm your solution.

5. Organizers for a party plan to serve at least 120 pounds of meat. The roast beef costs \$5 per pound and the chicken costs \$3 per pound. The organizers have a budget of at most \$600 for meat for the party. What are the possible amounts of roast beef and chicken?

*(N.B. This problem is featured on mathchamber.com/Unit 6 in the VIDEO TUTOR lesson entitled “Using a system of linear inequalities”)*

- a) Write **TWO** inequalities that describe this situation.  
Let the horizontal axis represent “***b***” – the pounds of roast beef.  
Let the vertical axis represent “***c***” – the pounds of chicken.



- b) Sketch a graph of the boundary lines and shade the region of the graph that shows the possible solutions for total money raised.
- c) **Shade your solution set** and **LABEL BOTH AXES accordingly**.
- d) Use the **TEST POINTS** method to confirm your solution.

*this problem adapted from the Pearson/Discovery Video Tutor Lesson “Using a system of linear inequalities”*